

Cardinal: Analytic tools for mass spectrometry imaging

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1 Introduction

The *R* package *Cardinal* has been created to fill the need for an efficient, open-source tool for the analysis of imaging data—specifically mass spectrometry imaging data. *Cardinal* is built upon data structures which follow Bioconductor (<http://www.bioconductor.org/>) standards for data classes in order to provide an additional level of convenience and familiarity to those who may be used to performing bioinformatic analyses in *R*.

Analysis in imaging data includes many things, such as visualization, pre-processing, and multivariate statistical techniques. Both supervised and unsupervised statistical methods are supported in *Cardinal*, including image segmentation (clustering), principle components analysis, and classification techniques such as partial least Squares discriminant analysis.

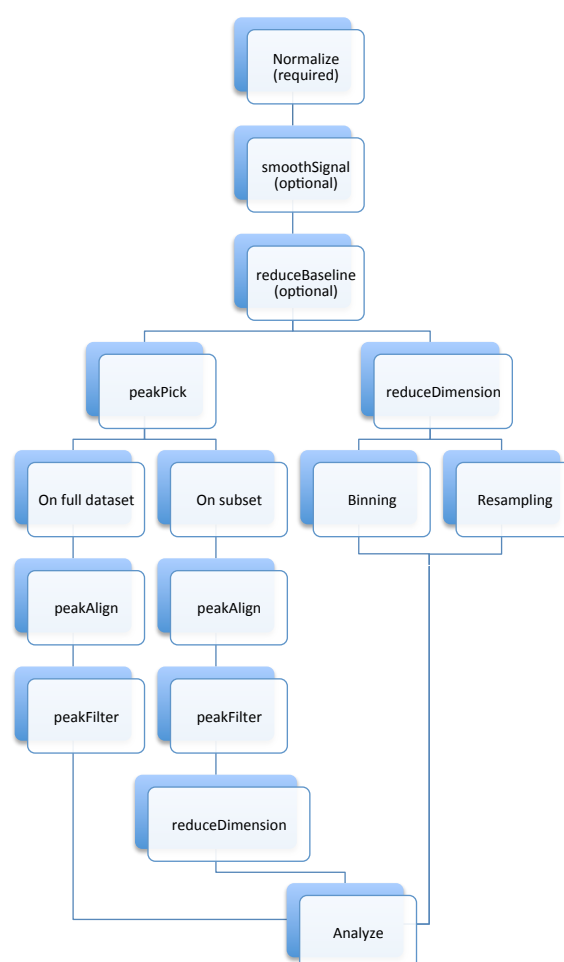


Figure 1: Cardinal workflow for pre-processing and analysis

Figure 1 charts out the workflow for mass spectrometry imaging data analysis.

This is a brief walkthrough of some of the basic functionality of *Cardinal*. For a more detailed view of the functionality of a given method, see the *R* help file.

Additional *R* packages useful for the analysis of mass spectrometry experiments are *MSnbase* [1] and *MALDIquant* [2], which are both designed for traditional proteomics analyses. *MALDIquant* also has limited support for mass spectrometry imaging data.

2 Input/Output

2.1 Input

In order to be analyzed in *Cardinal*, input data must be in either Analyze 7.5 and imzML format. These are two of the most common data exchange formats in imaging mass spectrometry.

2.1.1 Analyze 7.5

Originally designed for MRI data by the Mayo Clinic, Analyze 7.5 is a common format used for exchange of mass spectrometry imaging data.

The Analyze format uses a collection of three files with extensions `.hdr`, `.img`, and `.t2m` to store data. To read datasets stored in the Analyze format, use the `readAnalyze` function. All three files must be present in the same folder and have the same name (except for the file extension) for the data to be read properly.

```
> name <- "This is the common name of your .hdr, .img, and .t2m files"
> folder <- "/This/is/the/path/to/the/folder/containing/the/files"
> data <- readAnalyze(name, folder)
```

Large Analyze files can also be attached on-disk without fully loading them into memory by using the `attach.only=TRUE` option. Not all *Cardinal* features are supported for on-disk datasets.

For more information on reading Analyze files, type `?readAnalyze`.

2.1.2 imzML

The open XML-based format imzML is a more recently developed format specifically designed for interchange of mass spectrometry imaging datasets [3]. Many other formats can be converted to imzML with the help of free applications available online. See <http://www.imzml.org> for more information and links to free converters.

The imzML format uses two files with extensions `.imzML` and `.ibd` to store data. To read datasets stored in the imzML format, use the `readImzML` function. Both files must be present in the same folder and have the same name (again, except for the file extension) for the data to be read properly.

```
> name <- "This is the common name of your .imzML and .ibd files"
> folder <- "/This/is/the/path/to/the/folder/containing/the/files"
> data <- readImzML(name, folder)
```

Large imzML files can also be attached on-disk without fully loading them into memory by using the `attach.only=TRUE` option. Not all *Cardinal* features are supported for on-disk datasets.

Both 'continuous' and 'processed' imzML format are supported, but currently only 'continuous' format can be attached using `attach.only=TRUE`.

For more information on reading imzML files, type `?readImzML`.

2.1.3 readMSIData

Cardinal also provides the convenience function `readMSIData`, which can automatically recognize the whether the data format is Analyze or imzML based on file extensions. The same rules for naming conventions apply as described above, but one need only provide the path to any of the data files. For example, to read an Analyze file, providing the path to any of the `.hdr`, `.img`, or `.t2m` will work. Likewise, providing the path to either the `.imzML` or `.ibd` file will work for reading data stored in the imzML format.

```
> file <- "/This/is/the/path/to/an/imaging/data/file.extension"
> data <- readMSIData(file)
```

2.2 Output

2.2.1 RData files

Any *R* object, including those created by *Cardinal*, can be saved as an **RData** file using the `save` and loaded using the `load` function.

```
> save(data, file="/Where/to/save/the/data.RData")  
> load("/Where/to/save/the/data.RData")
```

When an **RData** file is loaded, the saved object appears in the global environment for the *R* session and is available for access by name, just as it was in the session during which it was saved. This functionality is part of *R*; see `?save` and `?load` for more details.

3 Data exploration and visualization

Mass spectrometry imaging datasets in *Cardinal* are stored in `MSImageSet` objects. This allows *Cardinal* to keep track of the spectra, pixel coordinates, m/z values and more in one place for the dataset. The `MSImageSet` object is described in more detail below. There are many methods for both creating and manipulating `MSImageSet` objects in *Cardinal*. We now describe some of these methods.

3.1 An example dataset

To illustrate methods for the `MSImageSet` objects, we begin by creating a simple, simulated dataset using the *Cardinal* function `generateImage`. This dataset will be the running example for this section. For more details on simulating mass spectrometry images, see `?generateImage` or Section 7.2 *Simulation*.

```
> pattern <- factor(c(0, 0, 2, 2, 0, 0, 0, 0, 0, 0, 2, 2, 0,
+ 0, 0, 0, 0, 0, 0, 1, 2, 2, 0, 0, 0, 0, 0, 2, 1, 1, 2,
+ 2, 0, 0, 0, 0, 0, 1, 2, 2, 2, 2, 0, 0, 0, 0, 1, 2, 2,
+ 2, 2, 2, 0, 0, 0, 0, 2, 2, 2, 2, 2, 2, 2, 0, 0, 0, 2,
+ 2, 0, 0, 0, 0, 0, 0, 2, 2, 0, 0, 0, 0, 0, 0),
+ levels=c(0,1,2), labels=c("blue", "black", "red"))
> set.seed(1)
> msset <- generateImage(pattern, coord=expand.grid(x=1:9, y=1:9),
+ range=c(1000, 5000), centers=c(2000, 3000, 4000),
+ resolution=100, step=3.3, as="MSImageSet")
> summary(msset)
```

```
Class: MSImageSet
Features: m/z = 1000 ... m/z = 4999.6 (1213 total)
Pixels: x = 1, y = 1 ... x = 9, y = 9 (81 total)
x: 1 ... 9
y: 1 ... 9
Size in memory: 1 Mb
```

The above code creates a simulated MS imaging dataset called `msset`, which is 9×9 pixels, with a mass range from m/z 1000 to m/z 5000. There are three peaks, occurring at m/z 2000, m/z 3000, and m/z 4000. Each of these peaks corresponds to a distinct region of interest. These are saved in the *factor* `pattern`. A *factor* is the standard way of storing categorical variables in *R*. All pixels with `pattern = 0` correspond to the region with peak at m/z 2000, `pattern = 1` corresponds to the peak at m/z 3000, and `pattern = 2` corresponds to m/z 4000.

We'll label these regions of interest "blue" pixels, "black" pixels, and "red" pixels, respectively.

3.2 The `MSImageSet` object

Most important aspects of a mass spectrometry imaging dataset stored in an `MSImageSet` object can be accessed by simple methods.

For example, m/z -values are accessed by the method `mz`, pixel coordinates are accessed by the method `coord`, and the mass spectra themselves are accessed by the method `spectra`. The mass spectra are stored as a matrix with each column corresponding to the mass spectrum at a single pixel.

```
> head(mz(msset), n=10) # first 10 m/z values
[1] 1000.0 1003.3 1006.6 1009.9 1013.2 1016.5 1019.8 1023.1 1026.4 1029.7

> head(coord(msset), n=10) # first 10 pixel coordinates
      x y
x = 1, y = 1 1 1
x = 2, y = 1 2 1
x = 3, y = 1 3 1
x = 4, y = 1 4 1
```

```

x = 5, y = 1 5 1
x = 6, y = 1 6 1
x = 7, y = 1 7 1
x = 8, y = 1 8 1
x = 9, y = 1 9 1
x = 1, y = 2 1 2

```

```
> head(spectra(msset)[,1], n=10) # first 10 intensities in the first mass spectrum
```

```
[1] 13.72308 11.93339 12.79512 12.50510 11.71788 13.92943 12.18719 12.24365 12.62183 12.30359
```

The methods `nrow` and `ncol` can be used to retrieve the number of features and number of pixels in an object, respectively. The method `dim` gives both number of features and number of pixels, while `dims` gives number of features as well as spatial dimensions of the image.

```
> nrow(msset)
```

```
Features
1213
```

```
> ncol(msset)
```

```
Pixels
81
```

```
> dim(msset)
```

```
Features  Pixels
1213      81
```

```
> dims(msset)
```

```
      iData
Features 1213
x         9
y         9
```

Two other helpful methods are `features` and `pixels`. These are useful for retrieving the feature number and pixel number (i.e., the row and column in the `spectra(msset)` matrix) corresponding to items of interest such as specific *m/z*-values or pixel coordinates.

```
> features(msset, mz=3000) # returns the feature number most closely matching m/z 3000
```

```
m/z = 2999.8
607
```

```
> mz(msset)[607]
```

```
[1] 2999.8
```

```
> pixels(msset, coord=list(x=5, y=5)) # returns the pixel number for x = 5, y = 5
```

```
x = 5, y = 5
41
```

```
> pixels(msset, x=5, y=5) # also returns the pixel number for x = 5, y = 5
```

```
x = 5, y = 5
41
```

```
> coord(msset)[41,]
```

```
      x y
x = 5, y = 5 5 5
```

See `?MSImageSet` for more details and additional methods.

Technical note: MSImageSet is an S4 class. It inherits from the more general SImageSet class, which itself inherits from the iSet virtual class. The iSet virtual class is designed around the same design principles as the eSet class provided by Biobase. See the “Cardinal development” vignette for more information.)

3.3 Subsetting a MSImageSet

A MSImageSet can be subset by row and column like an ordinary *R* matrix or *data.frame*, where rows correspond to the features (m/z -values) and columns correspond to pixels (locations associated with mass spectra). Subsetting will return a new MSImageSet.

For example, we can subset by m/z -values so that we only keep the mass range from m/z 2500 to m/z 4500.

```
> tmp <- msset[2500 < mz(msset) & mz(msset) < 4500,]
> range(mz(msset))
[1] 1000.0 4999.6
> range(mz(tmp))
[1] 2501.5 4498.0
```

Alternatively, we can subset by pixel coordinates. To keep only pixels with x -coordinates greater than 5, we can do the following.

```
> tmp <- msset[,coord(msset)$x > 5]
> range(coord(msset)$x)
[1] 1 9
> range(coord(tmp)$x)
[1] 6 9
```

We can also subset in both ways at once.

```
> tmp <- msset[2500 < mz(msset) & mz(msset) < 4500, coord(msset)$x > 5]
> range(mz(tmp))
[1] 2501.5 4498.0
> range(coord(tmp)$x)
[1] 6 9
```

It is also possible to manually select a region of interest and use it to subset the dataset. This is done using the `select` method, which will be introduced in Section 3.5 *Plotting ion images*.

3.4 Plotting mass spectra

Mass spectra from an MSImageSet can be displayed using the `plot` method. To plot the mass spectrum at the first pixel of our MSImageSet, we do the following:

```
> plot(msset, pixel=1)
```

The result of which is shown in Figure 2a.

Instead of pixel number, we can specify a set of coordinates corresponding to the mass spectrum we want to plot. The following produces Figure 2b, which is the mean spectrum for the pixel at spatial location (5,5), and all other spectra within a 2 pixel neighborhood of that location.

```
> plot(msset, coord=list(x=5, y=5), plusminus=2)
```

Finally, we can plot multiple spectra at once, as shown in Figure 2c. This is done below by specifying a vector for the `pixel` argument. The plots are displayed simultaneously by setting `superpose = TRUE` and `key = TRUE` generates a legend. The `pixel.groups` here indicates that the pixels should be grouped by their classifications as encoded by the `pattern` factor. By default, *Cardinal* averages over spectra in the same group.

```
> mycol <- c("blue", "black", "red")
> plot(msset, pixel=1:ncol(msset), pixel.groups=pattern, superpose=TRUE, key=TRUE, col=mycol)
```

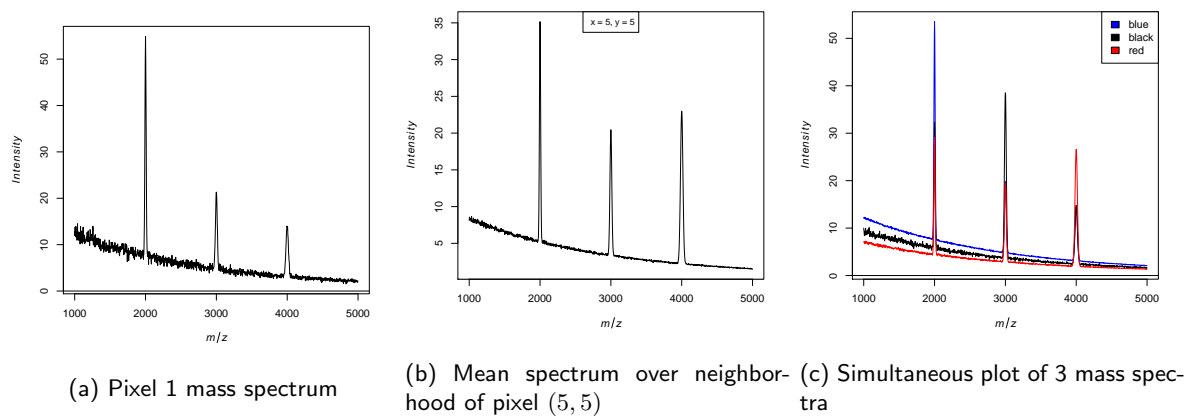


Figure 2: Plotting mass spectra.

3.5 Plotting ion images

Ion images from an `MSImageSet` can be plotted using the `image` method. To plot the ion image for the first feature, Figure 3a, we use:

```
> image(msset, feature=1)
```

The mean ion image for the neighborhood of m/z 4000 with radius 10, i.e. m/z [3990, 4010] is shown in Figure 3b.

```
> image(msset, mz=4000, plusminus=10)
```

In Figure 3c the ion images for m/z 2000, m/z 3000, and m/z 4000 are displayed simultaneously.

```
> mycol <- c("blue", "black", "red")
> image(msset, mz=c(2000, 3000, 4000), col=mycol, superpose=TRUE)
```

The ion image for m/z 2000 is shown in Figure 3d, with a custom color scale from white to blue. The most intense “hotspots” are suppressed.

```
> mycol <- gradient.colors(100, start="white", end="blue")
> image(msset, mz=2000, col.regions=mycol, contrast.enhance="suppress")
```

In Figure 3e, a smoothed ion image for m/z 3000 with a custom color scale from white to black is presented.

```
> mycol <- gradient.colors(100, start="white", end="black")
> image(msset, mz=3000, col.regions=mycol, smooth.image="gaussian")
```

Finally, in Figure 3f, for only those pixels defined as being from the “black” and “red” regions, we plot the ion image of m/z 4000 with a custom color scale from black to red.

```
> msset2 <- msset[,pattern == "black" | pattern == "red"]
> mycol <- gradient.colors(100, start="black", end="red")
> image(msset2, mz=4000, col.regions=mycol)
```

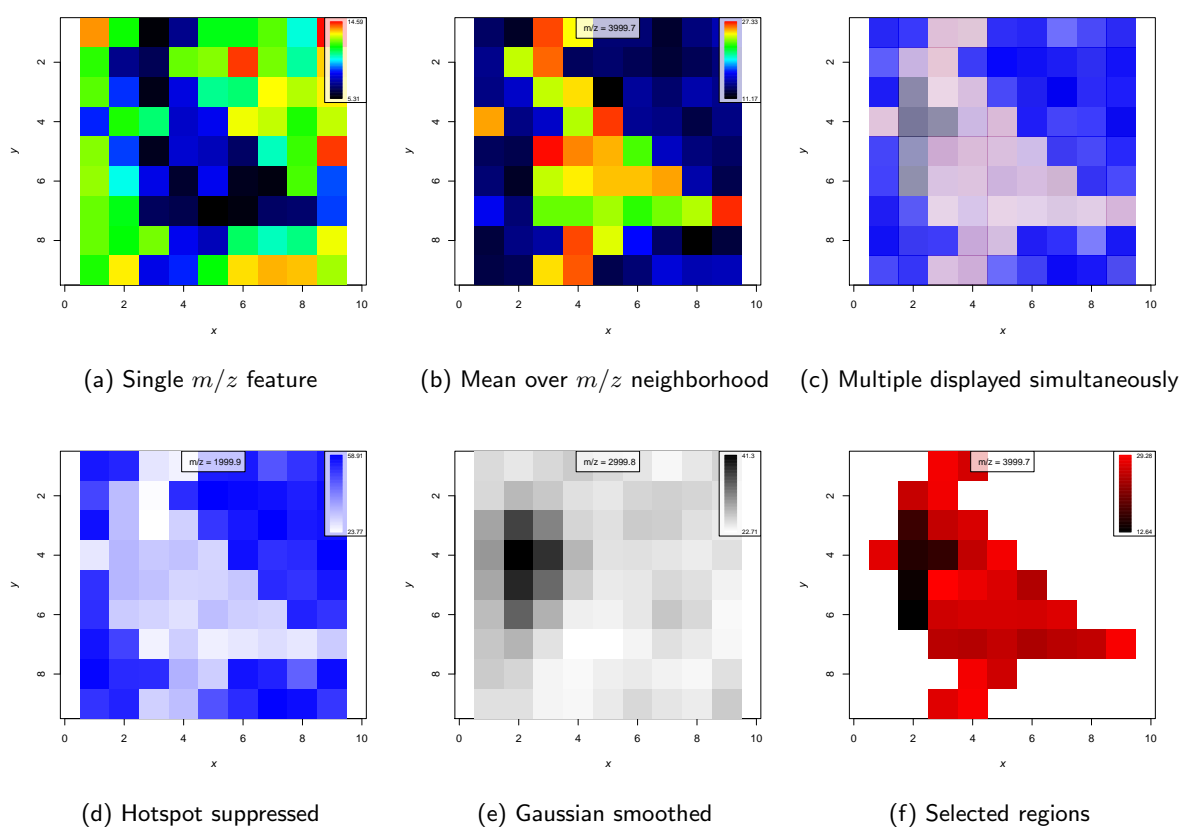



Figure 3: Plotting ion images.

4 Pre-processing

4.1 Normalization

Normalization is perhaps the most important pre-processing step before any kind of analysis should be performed on biological datasets, and mass spectrometry imaging experiments are no different in this regard. *Cardinal* provides normalization to total ion current (TIC), commonly used in MSI analysis (see [4] for a discussion of this method). In the first command below, we only perform the normalization on the first pixel in order to show a plot of the processing results in Figure 4. In the second, we perform normalization on the whole dataset.

```
> normalize(msset, pixel=1, method="tic", plot=TRUE)
> msset2 <- normalize(msset, method="tic")
```

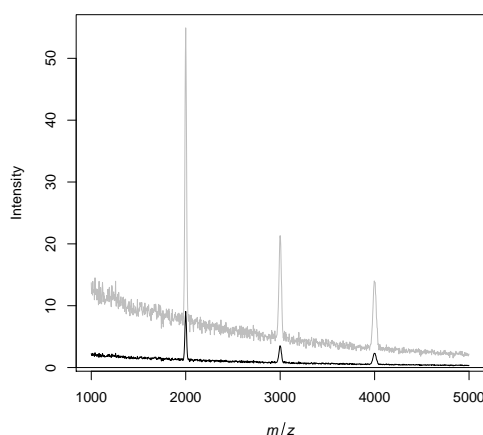


Figure 4: Total ion current (TIC) normalization.

4.2 Smoothing

Smoothing the mass spectra is useful for reducing noise, which can improve detection of peaks. *Cardinal* provides several common methods for smoothing mass spectra, including Gaussian kernel smoothing (Figure 5a), Savitsky-Golay smoothing (Figure 5b), and a simple moving average filter [5].

```
> smoothSignal(msset2, pixel=1, method="gaussian", window=9, plot=TRUE)
> smoothSignal(msset2, pixel=1, method="sgolay", window=15, plot=TRUE)
> msset3 <- smoothSignal(msset2, method="gaussian", window=9)
```

4.3 Baseline reduction

Baseline reduction is often necessary for many datasets, especially those obtained through matrix-assisted methods such as MALDI ([5]). *Cardinal* implements a simple version that interpolates a baseline from local medians or local minima, while attempting to preserve the signal from mass spectral peaks. Figure 6 shows baseline reduction for a single pixel, where the green curve represents the estimated baseline and the baseline-reduced spectrum is plotted in black.

```
> reduceBaseline(msset3, pixel=1, method="median", blocks=50, plot=TRUE)
```

We can also reduce baseline across all pixels in the image.

```
> msset4 <- reduceBaseline(msset3, method="median", blocks=50)
```

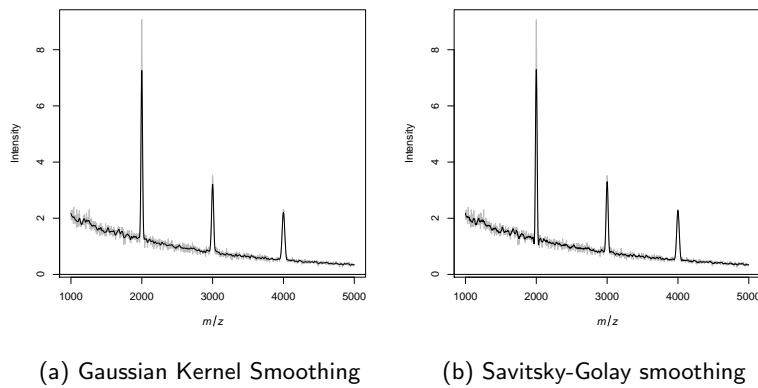


Figure 5: Smoothing techniques.

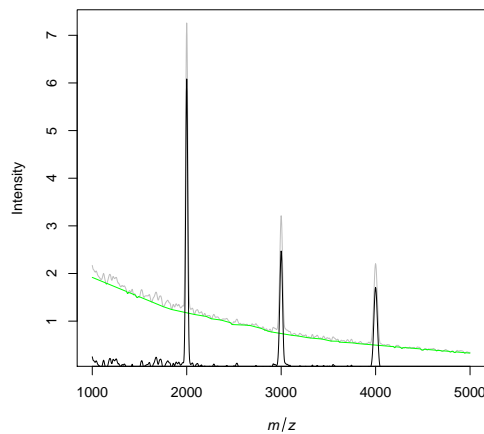


Figure 6: Baseline reduction using interpolation from medians.

4.4 Peak picking

Peak picking is a common form of data reduction that reduces the signal to relevant data peaks. *Cardinal* implements three varieties based on a user-specified signal-to-noise ratio (SNR). The “simple” version interpolates a constant noise pattern, the “adaptive” version interpolates an adaptive noise pattern Figure 7a, and “limpic” implements the LIMPIC algorithm for peak detection Figure 7b.

```
> peakPick(msset4, pixel=1, method="adaptive", SNR=3, plot=TRUE)
> peakPick(msset4, pixel=1, method="limpic", SNR=3, plot=TRUE)
> msset5 <- peakPick(msset4, method="simple", SNR=3)
```

4.5 Peak alignment

Peak alignment is necessary to account for possible inaccuracy in m/z measurements. Peaks can be aligned to a reference list of known m/z values, or to the local maxima in the mean spectrum. Figure 8 denotes the selected peaks by red vertical lines, and aligns the local maxima of the mean spectra to these peaks, as in [6].

```
> peakAlign(msset5, pixel=1, method="diff", plot=TRUE)
> msset6 <- peakAlign(msset5, method="diff")
```

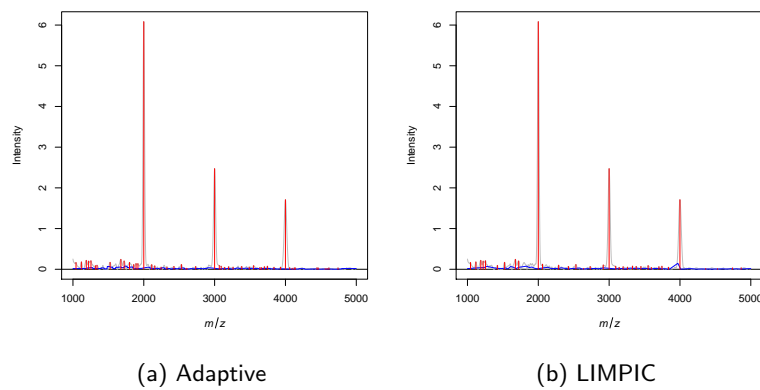


Figure 7: Peak picking techniques.

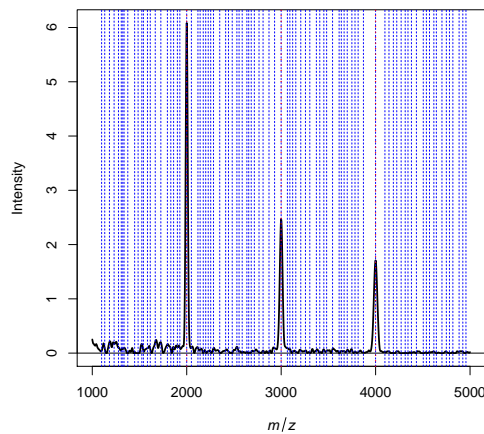


Figure 8: Peak alignment to the local maxima of the mean spectrum.

4.6 Peak filtering

Peak filtering removes peaks that occur infrequently, such as those which only occur in a small proportion of pixels. This is useful for removing extraneous peaks that are likely to be false positives.

```
> msset7 <- peakFilter(msset6, method="freq")
> dim(msset6) # 89 peaks retained
```

```
Features  Pixels
      89      81
```

```
> dim(msset7) # 10 peaks retained
```

```
Features  Pixels
      10      81
```

4.7 Data reduction

Other common forms of data reduction include resampling and binning.

Cardinal can do binning for a fixed width, taken to be 25 in this example. The mean intensity of ions located in the same m/z bin is taken to be the response in the reduced version of the data. The results of binning on pixel 1 is plotted in Figure 9a. The original spectrum is plotted in black, with the binned version displayed simultaneously in red.

```
> reduceDimension(msset4, pixel=1, method="bin", width=25, units="mz", fun=mean, plot=TRUE)
```

There is also the option of doing resampling for a fixed step size. The results of resampling with step size 25 m/z on pixel 1 is plotted in Figure 9b. The original spectrum is plotted in black, with the resampled version displayed simultaneously in red.

```
> reduceDimension(msset4, pixel=1, method="resample", step=25, plot=TRUE)
```

Data reduction can be done on the whole dataset at once.

```
> msset8 <- reduceDimension(msset4, method="resample", step=25)
```

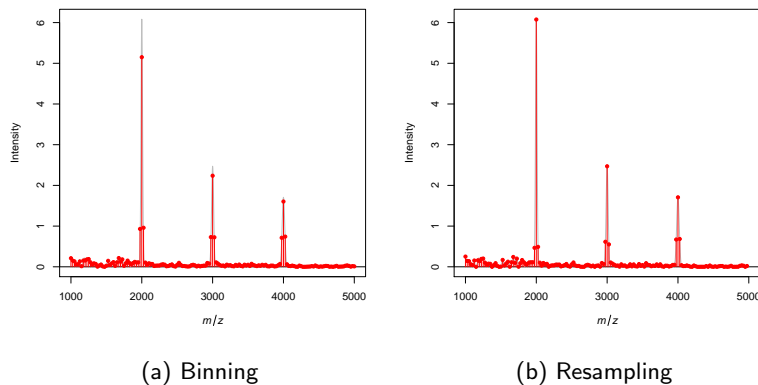


Figure 9: Data reduction via binning and resampling.

4.8 Batch processing

To simplify the above pre-processing steps, as well as save memory when processing on-disk data, *Cardinal* provides a batch processing method.

```
> msset9 <- batchProcess(msset, normalize=TRUE, smoothSignal=TRUE, reduceBaseline=TRUE)
> summary(msset9)
```

```
Class: MSImageSet
Features: m/z = 1000 ... m/z = 4999.6 (1213 total)
Pixels: x = 1, y = 1 ... x = 9, y = 9 (81 total)
x: 1 ... 9
y: 1 ... 9
Size in memory: 1 Mb
```

```
> processingData(msset9)
```

```
Processing data
Cardinal version: 1.6.0
Files:
Normalization: tic
Smoothing: gaussian
Baseline reduction: median
Spectrum representation:
Peak picking:
```

Each step can be set to its default parameters by setting it to TRUE, or a list of options can be provided.

```
> msset10 <- batchProcess(msset, normalize=TRUE, smoothSignal=TRUE, reduceBaseline=list(blocks=200),
+   peakPick=list(SNR=12), peakAlign=TRUE)
> summary(msset10)
```

```
Class: MSImageSet
Features: m/z = 1108.9 ... m/z = 4989.7 (139 total)
```

```
Pixels: x = 1, y = 1 ... x = 9, y = 9 (81 total)
x: 1 ... 9
y: 1 ... 9
Size in memory: 0.2 Mb
```

```
> processingData(msset10)
```

```
Processing data
```

```
Cardinal version: 1.6.0
```

```
Files:
```

```
Normalization: tic
```

```
Smoothing: gaussian
```

```
Baseline reduction: median
```

```
Spectrum representation: centroid
```

```
Peak picking: simple
```

This method is particularly useful when processing larger-than-memory on-disk datasets to a smaller processed form, without loading the full data into memory.

See `?batchProcess` for more details and differences in behavior from the individual processing methods.

5 Analysis

For example workflows with analyses of real datasets, please see the vignettes in the companion data package *CardinalWorkflows*.

5.1 Principal components analysis (PCA)

Principal components analysis (PCA) is a multivariate statistical tool used for dimension reduction and exploratory data analysis. PCA can be useful when first exploring a dataset beyond plotting molecular ion images, but additional statistical analysis is usually necessary to extract meaningful results.

Below, we fit the first two principal components using *Cardinal*'s PCA method and plot their loadings and scores.

```
> pca <- PCA(msset4, ncomp=2)
> plot(pca)
> image(pca)
```

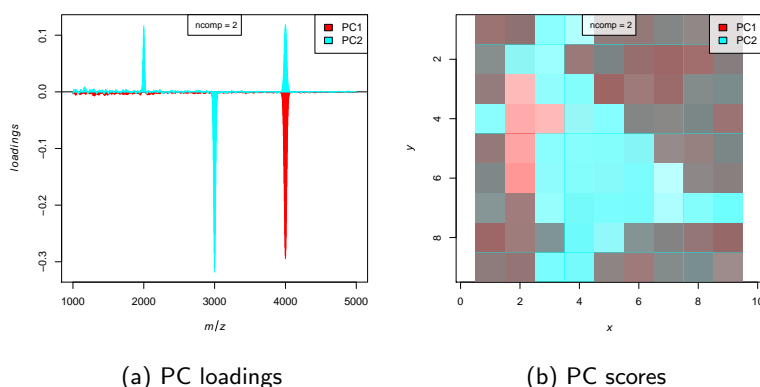


Figure 10: Principal components analysis.

See `?PCA` for more details.

5.2 Partial least squares (PLS)

Partial least squares (PLS), also called projection to latent structures, is a multivariate method from chemometrics that has been shown to be useful for classification of mass spectrometry images [7].

When used for classification, it is known as partial least squares discriminant analysis, or PLS-DA. PLS-DA works similarly to PCA, but it is a supervised method, so it requires data annotated with known labels.

Here, we train a PLS classifier using the `pattern` variable from earlier as our labels, and plot the results.

```
> pls <- PLS(msset4, y=pattern, ncomp=2)
> plot(pls, col=c("blue", "black", "red"))
> image(pls, col=c("blue", "black", "red"))
```

When working with classification on real data, cross-validation should always be used, using the `cvApply` method, to avoid biased results. See `?cvApply` and `?PLS` for more details.

5.3 Orthogonal partial least squares (O-PLS)

Orthogonal partial least squares (O-PLS) is a variation on PLS. O-PLS can sometimes improve the interpretability of the PLS model coefficients, while producing similar accuracy. O-PLS-DA is also implemented in *Cardinal*

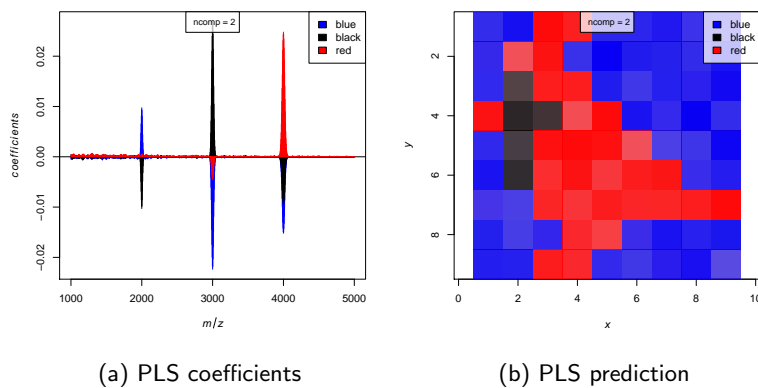


Figure 11: Partial least squares.

```
> oppls <- OPLS(msset4, y=pattern, ncomp=2)
> plot(oppls, col=c("blue", "black", "red"))
> image(oppls, col=c("blue", "black", "red"))
```

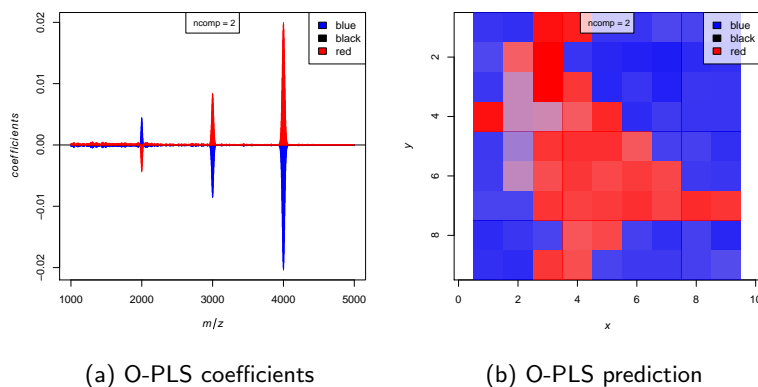


Figure 12: Orthogonal partial least squares.

O-PLS is primarily useful when many PLS components are required to fit an accurate model, since this often leads to unstable model coefficients. Try O-PLS when the PLS model coefficients are difficult to interpret, or the best PLS model uses a large number of components. See `?OPLS` for more details.

5.4 Spatially-aware k-means clustering

Spatially-aware clustering using k-means is available [6] through the `spatialKMeans` method. This method uses a spatial distance function to project the data to a kernel space before performing ordinary k-means clustering.

The parameters `r` and `k` are the neighborhood smoothing radius and the initial number of clusters.

Below, we create a spatial segmentation using spatially-aware clustering.

```
> set.seed(1)
> skm <- spatialKMeans(msset7, r=2, k=3, method="adaptive")
> plot(skm, col=c("black", "blue", "red"), type=c('p','h'), key=FALSE)
> image(skm, col=c("black", "blue", "red"), key=FALSE)
```

See `?spatialKMeans` for more details.

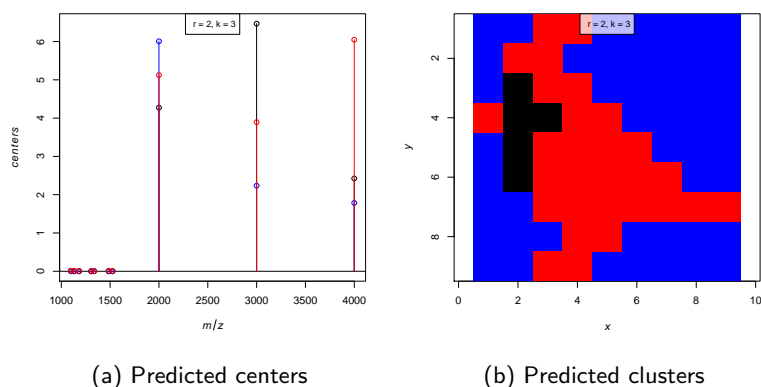


Figure 13: Spatially-aware k-means clustering.

5.5 Spatial shrunken centroids

Cardinal offers a novel clustering and classification method based on the spatial smoothing [6] and nearest shrunken centroids [8]. This is the `spatialShrunkenCentroids` method, which can be used both for clustering and for classification.

The parameters `r`, `k`, and `s` are the neighborhood smoothing radius, the initial number of clusters, and the sparsity parameter, respectively.

Below, we create a spatial segmentation using the spatial shrunken centroids method.

```
> set.seed(1)
> ssc <- spatialShrunkenCentroids(msset7, r=1, k=5, s=3, method="adaptive")
> plot(ssc, col=c("blue", "red", "black"), type=c('p','h'), key=FALSE)
> image(ssc, col=c("blue", "red", "black"), key=FALSE)
```

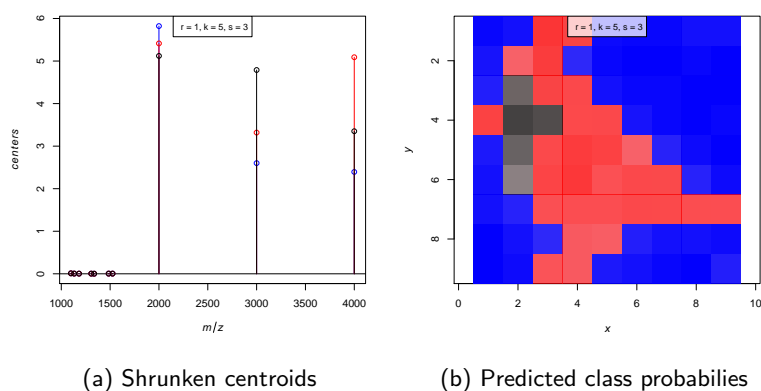


Figure 14: Spatially-aware nearest shrunken centroids clustering.

A unique property of *Cardinal*'s spatial shrunken centroids method is that it allows for the automated selection of the number of clusters, driven in part by the sparsity parameter. Although we initialized the clustering above with 5 clusters, only 3 were used in the final segmentation.

See `?spatialShrunkenCentroids` for more options and details.

6 Examples

In-depth biological examples using real data can be found in the *CardinalWorkflows* package. Figure 15 shows an example using a cross-section of a whole pig fetus, and Figure 16 shows an example using a human renal cell carcinoma dataset. Both datasets and a thorough walkthrough of analyses are available in *CardinalWorkflows*.

To install *CardinalWorkflows*, run:

```
> source("http://bioconductor.org/biocLite.R")
> biocLite("CardinalWorkflows")
```

Please note that due to the size of the included datasets, downloading and installing *CardinalWorkflows* may take a long time.

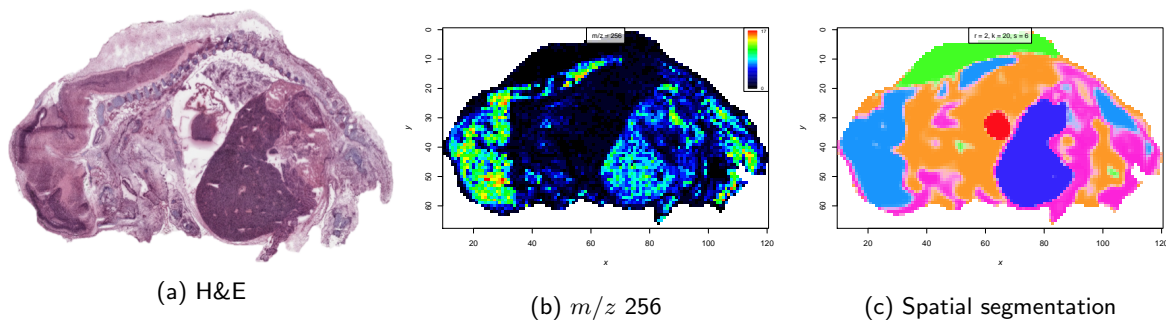


Figure 15: Biological example of a pig fetus cross-section, showing the optical image, an ion image, and a segmentation created by Spatial Shrunk Centroids clustering.

Figure 15 uses a pig fetus cross-section as an example of unsupervised analysis of a mass spectrometry imaging experiment using *Cardinal*. To view the vignette associated with this dataset, install *CardinalWorkflows* and run:

```
> vignette("Workflows-clustering")
```

The dataset and its analyses can be loaded by running:

```
> data(pig206, pig206_analyses)
```

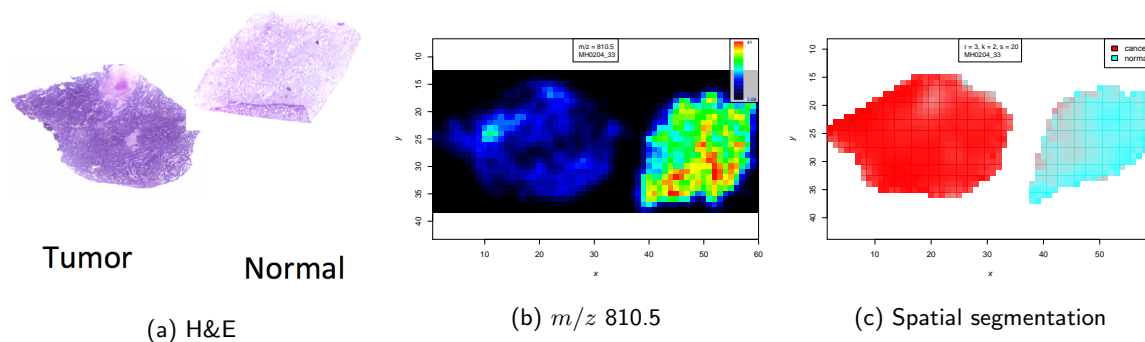


Figure 16: Biological example of human renal cell carcinoma classification, showing an optical image, an ion image, and a segmentation created by Spatial Shrunk Centroids classification.

Figure 16 uses a human renal cell carcinoma dataset as an example of supervised analysis of a mass spectrometry imaging experiment using *Cardinal*. To view the vignette associated with this dataset, install *CardinalWorkflows* and run:

```
> vignette("Workflows-classification")
```

The dataset and its analyses can be loaded by running:

```
> data(rcc, rcc_analyses)
```

See `?CardinalWorkflows` for more information.

7 Advanced Topics

7.1 Apply

The `apply` family of functions are a powerful feature of *R*. The `apply` function applies a function over margins of an array, while `sapply` applies a function over every element of a vector-like object. The function `tapply` applies a function over a “ragged” array, so that the function is applied over groups of values given by levels of another variable (usually a factor). In *Cardinal*, the methods `pixelApply` and `featureApply` allow `apply`-like functionality that combine traits of each of these, tailored for imaging datasets.

We need to mark which pixels are blue, black, and which are red, as in the *factor* pattern in Section 3.1.

```
> pData(msset)$pg <- pattern
```

Then we need to mark which features (which regions of the mass spectrum) belong to the peaks associated with “blue” (m/z 2000), “black” (m/z 3000), or “red” (m/z 4000) pixels; the rest of the spectrum is marked as background noise (bg).

```
> fData(msset)$fg <- factor(rep("bg", nrow(fData(msset)))), levels=c("bg", "blue", "black", "red"))
> fData(msset)$fg[1950 < fData(msset)$mz & fData(msset)$mz < 2050] <- "blue"
> fData(msset)$fg[2950 < fData(msset)$mz & fData(msset)$mz < 3050] <- "black"
> fData(msset)$fg[3950 < fData(msset)$mz & fData(msset)$mz < 4050] <- "red"
```

Now we can experiment with different ways of plotting an imaging dataset.

7.1.1 pixelApply

The method `pixelApply` allows functions to be applied over all pixels. The function is applied pixel-by-pixel to the feature vectors (mass spectra). Here, we use `pixelApply` to find the pixel-by-pixel mean intensity of different regions of the mass spectrum. We provide `fData(msset)$fg` as a grouping variable, since it indicates different regions of the mass spectrum we expect to be associated with either background noise, or blue, red, or black pixels. Since `pixelApply` knows to look in `msset` for the variable, we only need to provide `fg` to the argument `.feature.groups`.

```
> p1 <- pixelApply(msset, mean, .feature.groups=fg)
> p1[,1:30]
```

	x = 1, y = 1	x = 2, y = 1	x = 3, y = 1	x = 4, y = 1	x = 5, y = 1	x = 6, y = 1	x = 7, y = 1
bg	5.591239	5.516053	3.395579	3.185078	5.615956	5.650231	4.957623
blue	17.306620	17.046174	9.112457	8.557135	17.313809	17.481563	14.981038
black	9.974539	9.025602	8.412205	8.844019	9.631894	9.739096	8.005345
red	7.628184	7.010724	12.982994	12.059920	7.883425	7.838796	7.077551
	x = 8, y = 1	x = 9, y = 1	x = 1, y = 2	x = 2, y = 2	x = 3, y = 2	x = 4, y = 2	x = 5, y = 2
bg	5.285583	5.523104	5.173204	3.589339	3.361056	5.409369	5.962200
blue	16.141836	16.873337	15.842321	11.037839	8.760469	16.625576	18.391835
black	9.232942	9.679532	8.708974	8.632293	8.432287	9.626762	9.028662
red	7.870530	8.436895	7.819247	11.809760	12.806359	7.634099	7.807045
	x = 6, y = 2	x = 7, y = 2	x = 8, y = 2	x = 9, y = 2	x = 1, y = 3	x = 2, y = 3	x = 3, y = 3
bg	5.913981	5.710577	5.681514	5.860902	5.770548	4.274740	3.146736
blue	18.392521	17.591820	17.528622	18.254246	17.893589	11.131247	8.295846
black	10.234255	10.160928	10.370499	9.540406	10.013747	14.349932	7.718586
red	7.588946	7.244261	7.563269	7.941176	8.005526	8.245206	11.762278
	x = 4, y = 3	x = 5, y = 3	x = 6, y = 3	x = 7, y = 3	x = 8, y = 3	x = 9, y = 3	x = 1, y = 4
bg	3.316402	5.317308	5.688381	6.096776	5.727348	5.816680	3.290318
blue	9.750688	16.232286	17.530305	18.911349	17.500409	17.829095	9.134986
black	8.035290	9.444263	10.440994	10.710668	9.470964	9.166336	8.047249
red	12.332335	6.764745	8.139496	7.897016	8.365797	8.130600	12.516607
	x = 2, y = 4	x = 3, y = 4					
bg	4.533675	4.376095					
blue	11.546565	11.061959					

```
black    15.589934    14.972439
red      7.659493     8.236587
```

By comparing side-by-side with the ground truth (which we have stored in the variable `pData(msset)$pg`), we see the result is as we expected. For “blue” pixels, the mean intensity of features belonging to the “blue”-associated peak (m/z 2000) is higher. For “black” pixels, the mean intensity of features belonging to the “black”-associated peak (m/z 3000) is higher. Finally, for “red” pixels, the mean intensity of features belonging to the “red”-associated peak (m/z 4000) is higher.

```
> cbind(pData(msset), t(p1))[1:30,c("pg", "blue", "black", "red")]
```

	pg	blue	black	red
x = 1, y = 1	blue	17.306620	9.974539	7.628184
x = 2, y = 1	blue	17.046174	9.025602	7.010724
x = 3, y = 1	red	9.112457	8.412205	12.982994
x = 4, y = 1	red	8.557135	8.844019	12.059920
x = 5, y = 1	blue	17.313809	9.631894	7.883425
x = 6, y = 1	blue	17.481563	9.739096	7.838796
x = 7, y = 1	blue	14.981038	8.005345	7.077551
x = 8, y = 1	blue	16.141836	9.232942	7.870530
x = 9, y = 1	blue	16.873337	9.679532	8.436895
x = 1, y = 2	blue	15.842321	8.708974	7.819247
x = 2, y = 2	red	11.037839	8.632293	11.809760
x = 3, y = 2	red	8.760469	8.432287	12.806359
x = 4, y = 2	blue	16.625576	9.626762	7.634099
x = 5, y = 2	blue	18.391835	9.028662	7.807045
x = 6, y = 2	blue	18.392521	10.234255	7.588946
x = 7, y = 2	blue	17.591820	10.160928	7.244261
x = 8, y = 2	blue	17.528622	10.370499	7.563269
x = 9, y = 2	blue	18.254246	9.540406	7.941176
x = 1, y = 3	blue	17.893589	10.013747	8.005526
x = 2, y = 3	black	11.131247	14.349932	8.245206
x = 3, y = 3	red	8.295846	7.718586	11.762278
x = 4, y = 3	red	9.750688	8.035290	12.332335
x = 5, y = 3	blue	16.232286	9.444263	6.764745
x = 6, y = 3	blue	17.530305	10.440994	8.139496
x = 7, y = 3	blue	18.911349	10.710668	7.897016
x = 8, y = 3	blue	17.500409	9.470964	8.365797
x = 9, y = 3	blue	17.829095	9.166336	8.130600
x = 1, y = 4	red	9.134986	8.047249	12.516607
x = 2, y = 4	black	11.546565	15.589934	7.659493
x = 3, y = 4	black	11.061959	14.972439	8.236587

We can manually construct the images corresponding to the mean intensity of the three peaks centered at m/z 2000, m/z 3000, and m/z 4000 and plot their images. This is shown in Figure 17

```
> tmp1 <- MSImageSet(spectra=t(as.vector(p1["blue",])), coord=coord(msset), mz=2000)
> image(tmp1, feature=1, col.regions=alpha.colors(100, "blue"), sub="m/z = 2000")

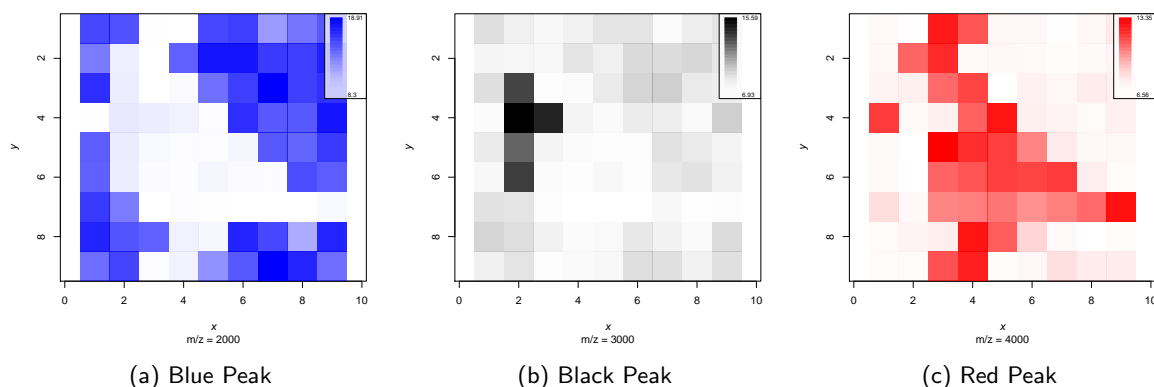
> tmp1 <- MSImageSet(spectra=t(as.vector(p1["black",])), coord=coord(msset), mz=3000)
> image(tmp1, feature=1, col.regions=alpha.colors(100, "black"), sub="m/z = 3000")

> tmp2 <- MSImageSet(spectra=t(as.vector(p1["red",])), coord=coord(msset), mz=4000)
> image(tmp2, feature=1, col.regions=alpha.colors(100, "red"), sub="m/z = 4000")
```

If only the plots are desired rather than the actual data, then `image` can be used to perform these steps automatically while producing the plot. See *Cardinal plotting* for how to do this.

7.1.2 featureApply

The method `featureApply` allows functions to be applied over all features. The function is applied to the flattened false-image vectors. These vectors are the pixel-by-pixel intensities of a single-feature image, not including

Figure 17: Mean intensities of the three peaks centered at m/z 2000, m/z 3000 and m/z 4000.

missing pixels. Here, we use `featureApply` to find the mean spectrum for different groups of pixels. We provide `pData(msset)$pg` as a grouping variable, since it indicates the kind of pixel. We desire mean spectra for the black pixels, the red pixels, and the blue pixels. As before, since `featureApply` knows to look in `msset`, we only need to provide `pg` to the argument `.pixel.groups`.

```
> f1 <- featureApply(msset, mean, .pixel.groups=pg)
> f1[,1:30]
```

	$m/z = 1000$	$m/z = 1003.3$	$m/z = 1006.6$	$m/z = 1009.9$	$m/z = 1013.2$	$m/z = 1016.5$	$m/z = 1019.8$
blue	12.113878	12.077172	12.271484	12.011245	12.106858	12.291783	12.011774
black	10.005194	9.491585	8.920648	8.395593	9.349371	8.972390	8.498503
red	7.019996	7.095126	7.206785	7.046938	6.770562	7.135863	6.915438
	$m/z = 1023.1$	$m/z = 1026.4$	$m/z = 1029.7$	$m/z = 1033$	$m/z = 1036.3$	$m/z = 1039.6$	$m/z = 1042.9$
blue	11.936433	12.210184	11.989588	11.848585	11.790103	12.031041	11.732924
black	9.054659	9.949408	8.628287	8.868370	8.991401	9.277913	8.660284
red	7.033159	7.091420	6.707759	7.258157	6.922927	7.025668	7.069312
	$m/z = 1046.2$	$m/z = 1049.5$	$m/z = 1052.8$	$m/z = 1056.1$	$m/z = 1059.4$	$m/z = 1062.7$	$m/z = 1066$
blue	11.867339	11.796285	11.848332	11.996489	11.853608	11.766950	12.006615
black	8.677262	9.554605	9.319258	8.995928	8.754828	9.730654	9.159634
red	7.120718	6.970966	6.852143	6.636296	6.992209	6.835762	6.493719
	$m/z = 1069.3$	$m/z = 1072.6$	$m/z = 1075.9$	$m/z = 1079.2$	$m/z = 1082.5$	$m/z = 1085.8$	$m/z = 1089.1$
blue	11.757288	11.696140	11.544314	11.550182	11.684293	11.747299	11.787957
black	8.890601	8.980763	10.102702	8.745331	9.359917	8.196362	9.204949
red	6.675064	6.787080	6.970741	6.662426	6.664785	6.829065	6.849054
	$m/z = 1092.4$	$m/z = 1095.7$					
blue	11.472797	11.710456					
black	9.279710	9.049170					
red	7.000153	6.704578					

Again, we can check the results by plotting them in Figure 18.

```
> plot(mz(msset), f1["blue",], type="l", xlab="m/z", ylab="Intensity", col="blue")
> plot(mz(msset), f1["black",], type="l", xlab="m/z", ylab="Intensity", col="black")
> plot(mz(msset), f1["red",], type="l", xlab="m/z", ylab="Intensity", col="red")
```

As expected, we see the mean spectrum of the blue pixels has a higher peak at m/z 2000, we see the mean spectrum of the black pixels has a higher peak at m/z 3000, while the mean spectrum of the red pixels has a higher peak at m/z 4000. As before, if only the plots are desired rather than the actual data, then `plot` can be used to perform these steps automatically. See *Cardinal plotting* for how to do this.

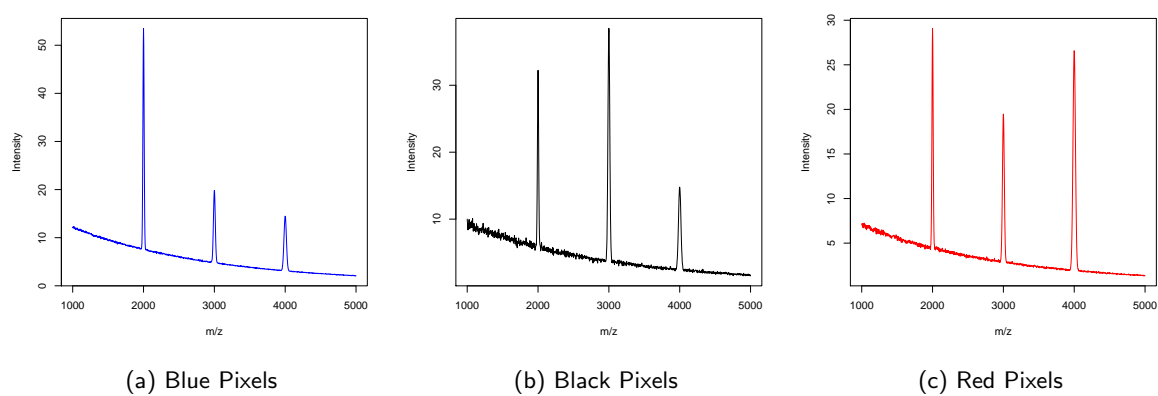


Figure 18: Mean spectra of blue, black, and red regions.

7.2 Simulation

Cardinal provides functions for the simulation of mass spectra and mass spectrometry imaging datasets. This is of interest to developers for testing newly developed methodology for analyzing mass spectrometry imaging experiments.

7.2.1 Simulation of spectra

The `generateSpectrum` function can be used to simulate mass spectra. Its parameters can be tuned to simulate different kinds of mass spectra from different kinds of machines, and different protein and peptide patterns.

One spectrum with m/z range from 1001 to 20000, 50 randomly selected peaks, baseline 3000, and m/z resolution 100 is generated below and plotted in Figure 19a.

```
> set.seed(1)
> s1 <- generateSpectrum(1, range=c(1001, 20000), centers=runif(50, 1001, 20000), baseline=2000, resolution=100)
> plot(x ~ t, data=s1, type="l", xlab="m/z", ylab="Intensity")
```

An example with fewer peaks, larger baseline, and lower resolution (Figure 19b):

```
> set.seed(2)
> s2 <- generateSpectrum(1, range=c(1001, 20000), centers=runif(20, 1001, 20000), baseline=3000, resolution=50)
> plot(x ~ t, data=s2, type="l", xlab="m/z", ylab="Intensity")
```

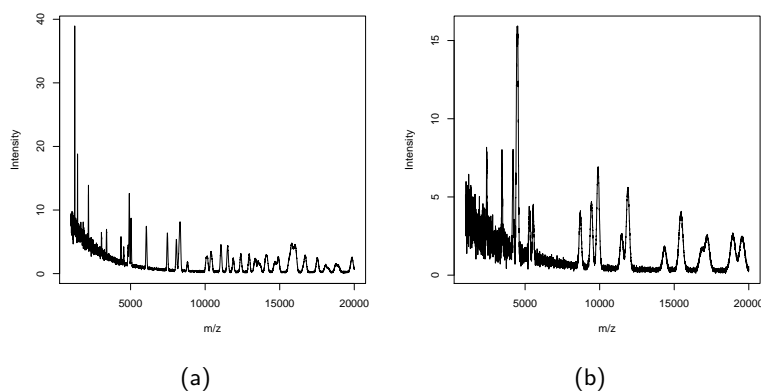


Figure 19: MALDI-like simulated spectra.

Above we simulated MALDI-like spectra. We can also simulate DESI-like spectra, shown in Figure 20.

```
> set.seed(3)
> s3 <- generateSpectrum(1, range=c(101, 1000), centers=runif(25, 101, 1000), baseline=0, resolution=25)
> plot(x ~ t, data=s3, type="l", xlab="m/z", ylab="Intensity")
> set.seed(4)
> s4 <- generateSpectrum(1, range=c(101, 1000), centers=runif(100, 101, 1000), baseline=0, resolution=5)
> plot(x ~ t, data=s4, type="l", xlab="m/z", ylab="Intensity")
```

7.2.2 Simulation of images

The `generateImage` function can be used to simulate mass spectral images. This is a simple wrapper for `generateSpectra` that will generate unique spectral patterns based on a spatial pattern. The generated mass spectra will have a unique peak associated with each region. The pattern must have discrete regions, most easily given in the form of an integer matrix. We use a matrix in the pattern of a cardinal.

```
> data <- matrix(c(NA, NA, 1, 1, NA, NA, NA, NA, NA, NA, 1, 1, NA, NA,
+ NA, NA, NA, NA, NA, 0, 1, 1, NA, NA, NA, NA, NA, 1, 0, 0, 1,
+ 1, NA, NA, NA, NA, NA, 0, 1, 1, 1, 1, NA, NA, NA, NA, 0, 1, 1,
```

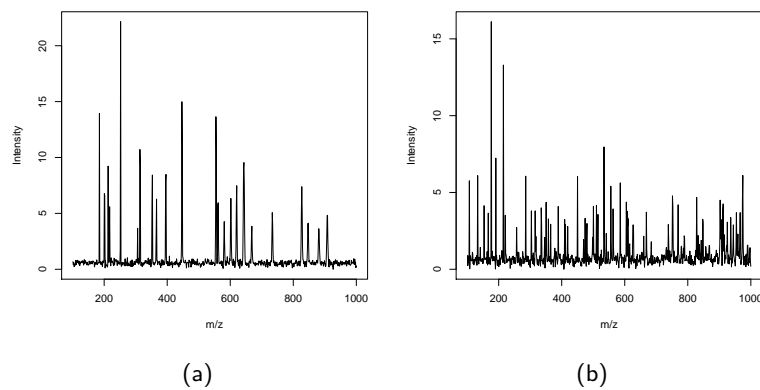


Figure 20: DESI-like simulated spectra.

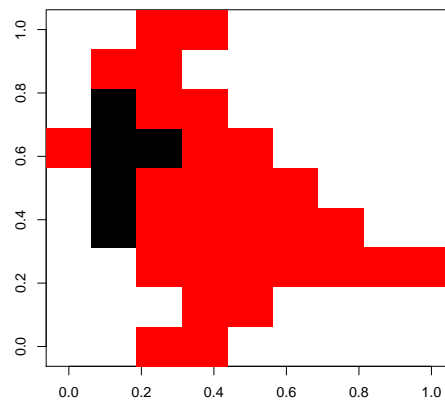


Figure 21: Ground truth image used to generate the simulated dataset.

```
+ 1, 1, 1, NA, NA, NA, NA, 1, 1, 1, 1, 1, 1, NA, NA, NA, 1,
+ 1, NA, NA, NA, NA, NA, NA, NA, 1, 1, NA, NA, NA, NA, NA), nrow=9, ncol=9)
```

As seen in Figure ??, we can plot the ground truth image directly.

```
> image(data[,ncol(data):1], col=c("black", "red"))
```

Now we generate the dataset. To make it easy to visualize, we set up the range and step size so that the feature indices correspond directly to their values. We create two peaks at m/z 100 and m/z 200, one of which is associated with each region in the image.

```
> set.seed(1)
> img1 <- generateImage(data, range=c(1,1000), centers=c(100,200), step=1, as="MSImageSet")
```

Now to confirm the reasonability of our simulated dataset, we plot images corresponding to the two peaks associated with each region in Figure 22b. (Note that rows in the original matrix correspond to the x-axis in the image and the columns correspond to the y-axis.)

```
> image(img1, mz=100, col.regions=alpha.colors(100, "black"))
> image(img1, mz=200, col.regions=alpha.colors(100, "red"))
```

We can generate the same kind of dataset using a factor and a data.frame of coordinates, as is done in the running example for earlier sections of this vignette.

```
> pattern <- factor(c(0, 0, 2, 2, 0, 0, 0, 0, 0, 0, 2, 2, 0,
+ 0, 0, 0, 0, 0, 0, 1, 2, 2, 0, 0, 0, 0, 0, 2, 1, 1, 2,
```

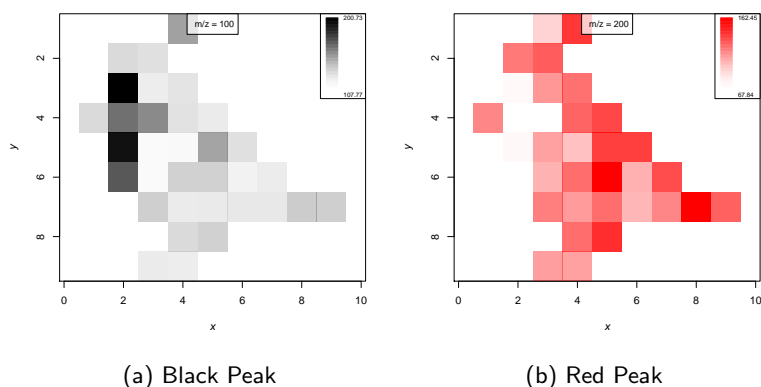



Figure 22: Generated image from an integer matrix.

```

+ 2, 0, 0, 0, 0, 0, 1, 2, 2, 2, 2, 0, 0, 0, 0, 1, 2, 2,
+   2, 2, 2, 0, 0, 0, 0, 2, 2, 2, 2, 2, 2, 2, 0, 0, 0, 2,
+   2, 0, 0, 0, 0, 0, 0, 2, 2, 0, 0, 0, 0, 0, 0, 0,
+   levels=c(0,1,2), labels=c("blue", "black", "red"))
> coord <- expand.grid(x=1:9, y=1:9)
> set.seed(2)
> msset <- generateImage(pattern, coord=coord, range=c(1000, 5000), centers=c(2000, 3000, 4000), resolu

```

Again, we can plot the images to see that the simulated dataset is the same pattern as before (though the exact intensities will differ, because we have used a different seed for the random number generator), Figure 23.

```

> image(msset, mz=2000, col.regions=alpha.colors(100, "blue"))
> image(msset, mz=3000, col.regions=alpha.colors(100, "black"))
> image(msset, mz=4000, col.regions=alpha.colors(100, "red"))

```

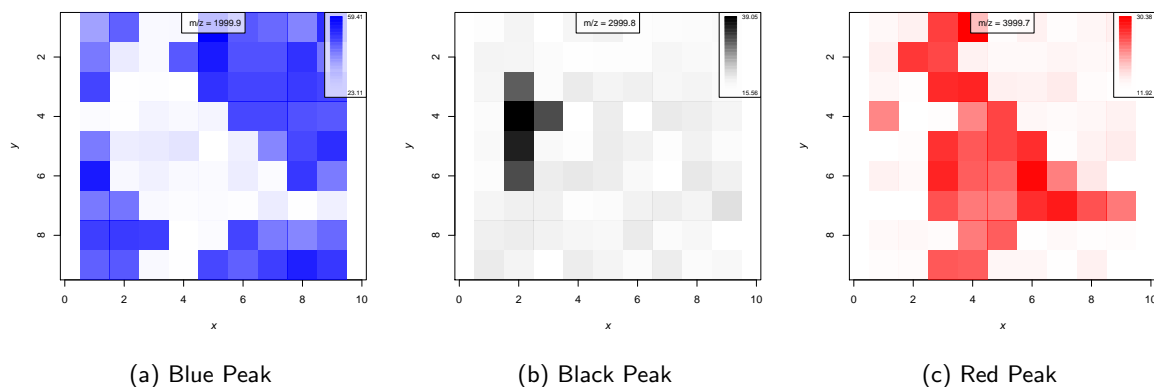


Figure 23: Generated images from factor and coordinates

7.2.3 Advanced simulation

The `generateImage` function provides a straightforward method for rapid simulation of many kinds of images to test classification and clustering models, but suppose we wish to simulate a more complex dataset with spatial correlations. Below we simulate a dataset with two overlapping regions. In each of these regions, the intensity degrades with distance from the center of the region, implying spatial correlation, Figure 24.

```

> x1 <- apply(expand.grid(x=1:10, y=1:10), 1,
+   function(z) 1/(1 + ((4-z[[1]])/2)^2 + ((4-z[[2]])/2)^2))

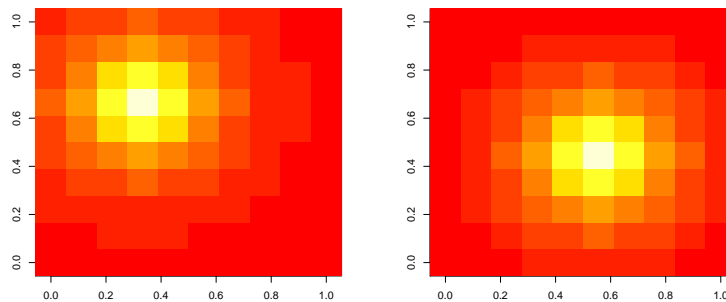
```

```

> dim(x1) <- c(10,10)
> image(x1[,ncol(x1):1])

> x2 <- apply(expand.grid(x=1:10, y=1:10), 1,
+             function(z) 1/(1 + ((6-z[[1]])/2)^2 + ((6-z[[2]])/2)^2))
> dim(x2) <- c(10,10)
> image(x2[,ncol(x2):1])

```



(a) Region 1

(b) Region 2

Figure 24: Ground truth images of a dataset with overlapping regions.

We generate the image by using `generateSpectrum` with the calculated mean intensities. We use two peaks for the two regions with nearly overlapping peaks at m/z 500 and m/z 510.

```

> set.seed(1)
> x3 <- mapply(function(z1, z2) generateSpectrum(1, centers=c(500,510), intensities=c(z1, z2), range=c(
> img3 <- MSIImageSet(x3, coord=expand.grid(x=1:10, y=1:10), mz=1:1000)

```

Now we can plot the ion images for each of the two peaks in 25.

```

> image(img3, mz=500, col=intensity.colors(100))
> image(img3, mz=510, col=intensity.colors(100))

```

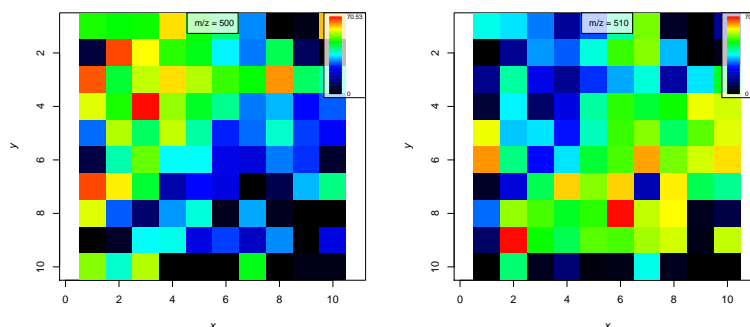
(a) Ion image for peak at m/z 500(b) Ion image for peak at m/z 510

Figure 25: Simulated mass spectral images at the two peaks.

Finally, we plot the mass spectrum for a pixel from each region in Figure 26

```

> plot(img3, coord=list(x=4, y=4), type="l", xlim=c(200, 800))
> plot(img3, coord=list(x=6, y=6), type="l", xlim=c(200, 800))

```

By creating spatial correlation patterns and combining them with the `intensities`, `sd`, and `noise` arguments in `generateSpectrum`, it is possible to simulate more complex mass spectrometry imaging datasets.

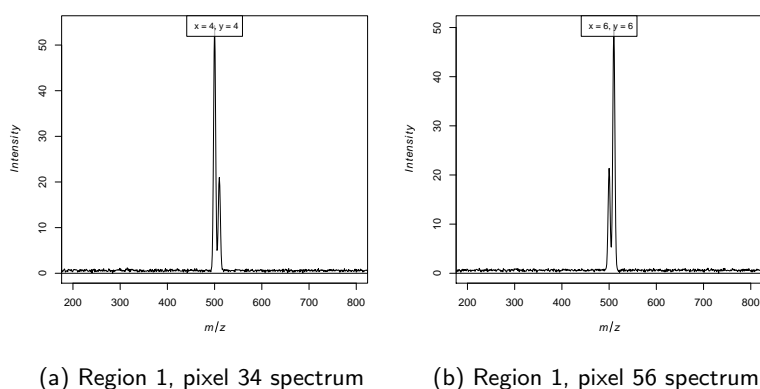


Figure 26: Simulated mass spectra from each of the two regions.

8 Session info

- R version 3.3.1 (2016-06-21), x86_64-w64-mingw32
- Locale: LC_COLLATE=C, LC_CTYPE=English_United States.1252, LC_MONETARY=English_United States.1252, LC_NUMERIC=C, LC_TIME=English_United States.1252
- Base packages: base, datasets, grDevices, graphics, methods, parallel, stats, utils
- Other packages: Biobase 2.34.0, BiocGenerics 0.20.0, Cardinal 1.6.0, ProtGenerics 1.6.0
- Loaded via a namespace (and not attached): BiocStyle 2.2.0, MASS 7.3-45, Matrix 1.2-7.1, grid 3.3.1, irlba 2.1.2, lattice 0.20-34, signal 0.7-6, sp 1.2-3, stats4 3.3.1, tools 3.3.1

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